

Technical Elective: Tensor Analysis in Materials

Instructor

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Meeting Time & Location

Friday 8:15-11:00 at RM 3-102

Zoom meeting for first a couple of weeks

(Zoom link: <https://us06web.zoom.us/j/81561303790?pwd=eC9LajlmdWRsbVdpdzFTb3p1RUl3QT09>)

Office Hour

Friday 13:00-15:00, or by appointment

TA information

Yu Liu: 2021223010040@stu.scu.edu.cn

WeChat group for Q&A, sending notices, ...

Scan the code in Blackboard to join the group.

Course Materials

Textbook

J. F. Nye, "Physical Properties of Crystals: Their Representation by Tensors and Matrices", Oxford University Press (1985)

Class notes

Handouts

Reference Textbooks

Robert E. Newnham, "Properties of materials: anisotropy, symmetry, structure", Oxford University Press (2005)

W. Michael Lai, David Rubin, Erhard Krempl, "Introduction to Continuum Mechanics", 3rd edition, Butterworth-Heinemann Ltd., Boston (1993)

Course Description

A comprehensive treatment of deformation-related physical behaviors of materials in the mathematical framework of tensor analysis. Development of elastic constitutive relations. Introduction to non-elastic strain associated with thermal expansion, ferroelectricity, and magnetism. Relations between material symmetry and tensor properties.

Course Objectives

Upon successful completion of this course, the students will be able to:

1. Utilize tensor algebra and calculus of tensor fields;
2. Understand stress, strain, and the constitutive relations;
3. Determine the effects of material symmetry on the physical properties;
4. Analyze the internal stress due to thermal expansion, electrostriction and magnetostriction.

Prerequisite

MATH 0280: Matrices and Linear Algebra

ENGR 0022: Materials Structures and Properties

MSE 1070: Mechanical Behavior of Materials (Preferred, not mandatory)

Grading

Homework	35%
Midterm Exam	30%
Final Exam	35%

Course Policies

1. Show up on time.
2. It is OK to discuss homework assignments with your classmates, but all submissions must be your own work.
3. It is expected that you will work on assignments consistently from the day they are made available.

Evaluation Policy

Partial credit will be awarded to recognize that some portion of the work is correct. However, partial credit grading is only practical if the work is clearly developed, with clear and well-marked diagrams when fitting, with the appropriate equations prominently displayed, where the substitutions into the equations are quite clear, and the assumptions used are obvious to the grader. That is, it is the student's responsibility to present her/his work so clearly that the grader can quickly ascertain the location and nature of the error(s) and can follow the subsequent work through. If this is not clear on the work submitted, credit cannot be given (then or later). ***Partial credit is assigned at the discretion of the grader.*** It is therefore always in your best interest to practice clarity and completeness in your solutions when working homework problems. This is applicable to exam problems as well.

Copyrights

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Academic Integrity

All students are expected to adhere to the standards of academic honesty. Any student engaged in cheating, plagiarism, or other acts of academic dishonesty would be subject to disciplinary action. Any student suspected of violating this obligation for any reason during the semester will be required to participate in the procedural process, initiated at the instructor level, as outlined in the University Guidelines on Academic Integrity. This may include but is not limited to the confiscation of the examination of any individual suspected of violating the University Policy.

Course Contents

Chapter 1 General Principles

- 1.1 Indicical notation
- 1.2 Vector
- 1.3 Tensor (second-rank)
- 1.4 Transformation laws
- 1.5 Eigenvalues and eigenvectors
- 1.6 Mohr circle

- 1.7 Examples of second-rank tensor
- 1.8 Material symmetry
- 1.9 Gradient, divergence, curl, and Gaussian theorem

Chapter 2 Stress

- 2.1 Force
- 2.2 Stress tensor
- 2.3 Conservation of linear momentum & moment of momentum
- 2.4 Proof that σ_{ij} form a tensor
- 2.5 Normal stress and shear stress
- 2.6 Mohr circle
- 2.7 Special forms of the stress tensor
- 2.8 Difference between the stress tensor and tensors representing crystal properties

Chapter 3 Strain

- 3.1 Description of motion
- 3.2 Deformation gradient
- 3.3 Lagrangian strain
- 3.4 Infinitesimal strain

Chapter 4 Elasticity

- 4.1 Hooke's law
- 4.2 Matrix notation/Voigt notion/contracted form
- 4.3 The effect of material symmetry
- 4.4 Young's modulus
- 4.5 Shear modulus, bulk modulus, and Poisson's ratio
- 4.6 Elastic properties of polycrystals
- 4.7 Stress-strain relation for an isotropic material
- 4.8 Navier equations

Chapter 5 Stress-free strain (spontaneous strain/eigenstrain)

- 5.1 Introduction
- 5.2 Thermal expansion
- 5.3 Strain mismatch at the "stress-free strain domain" boundaries (internal stress)
- 5.4 Electrostriction
- 5.5 Magnetostriction